## ANALITYCAL METHOD FOR DIMENSIONING DYNAMIC WDM OPTICAL NETWORKS

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#### **Basic System**

WDM network.

Dynamic

Each node is capable of converting wavelengths.

Objective: To offer P classes of service

- Class 1 is highest priority
- Class P is lowest priority

QoS definition:

Blocking Probability of the class  $k : B_k$ ;  $1 \le k \le P$ 

## Analysis for a link

Model

- W wavelengths
- arrival process of class k,  $1 \le k \le P$ :

Poisson process with rate  $\lambda_k$ 

The burst service time follows an exponential distribution of parameter μ, which is independent of the class.

## Analysis for a link

Strategie for offering differents QoS

- ■Users of class k, 1≤ k ≤ P, can transmit using only wavelengths 1 to M<sub>k</sub>
- Users of class k-1, transmit using the wavelengths 1 to M<sub>k-1</sub> (>M<sub>k</sub>)

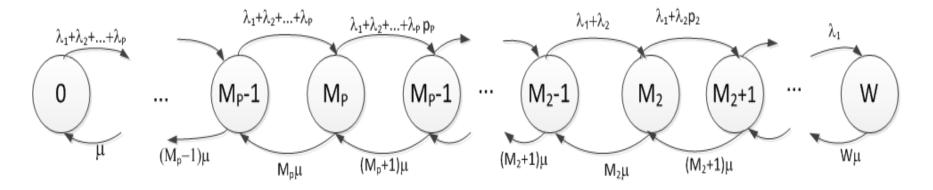
Users of class 1, transmit using wavelengths 1 to W

## Model Summary

The above considerations can be summarized in a Markovian model M / M / W / W. State= number of available wavelengths

$$\lambda_{k} = \begin{cases} \sum_{j=1}^{P} \lambda_{j} & ; & 0 \le k < M_{P} \\ \sum_{i=1}^{j} \lambda_{i} & ; & M_{j+1} < k < M_{j}; \ j \in \{1, \dots, P\} \\ \sum_{i=1}^{j-1} \lambda_{i} + \lambda_{j} p_{j} & ; & k = M_{j}; \ j \in \{1, \dots, P\} \end{cases}$$
(1)

$$\mu_k = k\mu$$



### Contribution of this work

- The thresholds procedure was published in [1]. However to obtain the results, the authors used Markov Decision Process, which is a complex method to evaluate computationally different thresholds.
- Next we derive a new and efficient way of find the different thresholds

[1] Li Yang and G. Rouskas, «Optimal Wavelength Sharing Policies in OBS networks Subject to QoS constraints, IEEE JSAC, (25) 9, 2007.

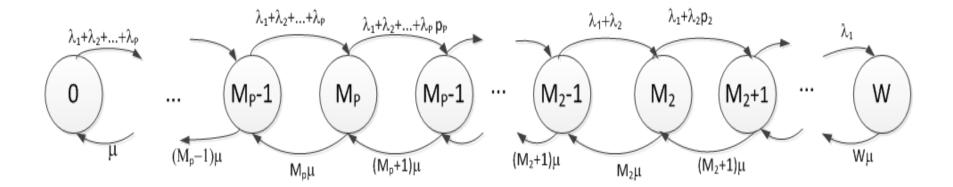
# **Model Solution**

 Considering that the previous markov chain is a birth death process, it is known that the recurrent solution of this queue is:

• From left to right: 
$$\pi_k = \pi_0 \prod_{j=1}^k \frac{\lambda_{j-1}}{\mu_j}$$
 (2)  
• From right to left:  $\pi_k = \pi_W \prod_{j=k}^{W-1} \frac{\mu_{j+1}}{\lambda_j}$  (3)

#### Design Goal

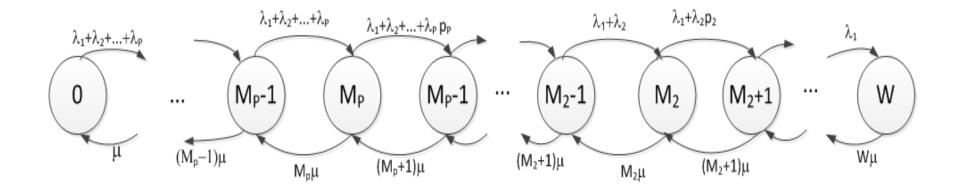
- To find the thresholds M<sub>k</sub>, M<sub>k-1</sub>, ..., M<sub>1</sub> such that qualities of service B<sub>k</sub>, B<sub>k-1</sub>, ..., B<sub>1</sub> of each class are met.
- For this, we consider the non normalized probabilities Pr(k)



#### Recurrent procedure

- $\Box \text{ Initially: } Pr(1)=1 \text{ ; (or } P(W)=1) \tag{4}$
- According to equations (2, 3 and 4) and the definitions of the different quality of services, the followig proportion must be satisfied:

$$\frac{\Pr(M_{k})}{B_{k}} = \frac{\Pr(M_{k-1})}{B_{k-1}}$$
 (5)



#### Recurrent procedure

□ The previous recurrent procedure allows the evaluation of all the thresholds:  $M_1, M_2, ..., M_P$ 

## **Final Remarks**

- Then, the contribution of this work consists in proposing the previous recurrent method,
- that allows evaluate the same thresholds in a (much) faster and simpler way.
- This is relevant, because the just described procedure must be applied a great number of times to solve more complex problems, like :
- End-to-end quality of service
- Routing problem, etc.